| Semester | 1 |
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| Course *1 | Minor |
| Paper Code | B1MT230111T |
| Paper Title | Calculus-1 and Vector Algebra \& Matrix Algebra [ Chem+Microbio+Biotech] |
| No. of Credits *2 | 4 |
| Theory / Practical / Composite | Theory |
| Minimum No. of preparatory hours per week a student has to devote | 4 |
| Number of Modules | 2 |
| Syllabus | Module-1 [Calculus-1] <br> 1. Infinite Sequence and Series [9]: Bounded, monotone and convergence sequence; Bounded monotone sequence converge (statement only): applications [3]. Convergence and divergence of a series. Necessary condition of convergence, Geometric \& p-series (statement only). Statement of tests of convergence of positive series: Comparison, D'Alembert, Cauchy, Raabe's Test: Applications [5]. Statement of Leibnitz Test for convergence of alternating series [1]. <br> 2. Differentiation and Mean Value theorems [16]: LHD \& RHD: examples, Sign of Derivative-monotone increasing and decreasing functions [4], Mean Value Theorems: Rolle's, Lagrange's and Cauchy's theorems and its applications [ no proof][5], Taylor's finite and infinite Series expansion, Application of the principle of maximum and minimum for a function of a single variable in geometrical, physical and other problems [4], Fourier Series: statement of Dirichlet's Theorem: examples [3]. <br> Module-2 [Vector Algebra \& Matrix Algebra] |


|  | 3. Vector Algebra and its applications to Geometry [16] Basic Vector operations [2], Multiplication of Vectors: Scalar and vector triple product [5], Vector Equations of different forms of planes and straight lines, shortest distance between lines, volume of tetrahedron [9] <br> 4. Matrices \& Determinants [11]: Unitary and Hermitian Matrices [3], Laplace's expansion method for determinants [1], rank of a matrix by elementary row operations [4], consistency of a system of linear equations. [3] |
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| Learning Outcomes *3 | On successful completion of this course a student will be able to do the following: <br> - Find whether the dependent variable is increasing/decreasing with increase in independent variable value and the rate of increment/decrement thereby understanding to finding of increment/decrement of a quantity with the change of dependant factor and applying to population dynamics and inferring about the same. <br> - Understand conditions under which mean value of two values of a variable is attained by that variable; will learn that if one knows a range for the velocity of a vehicle, a bound of its displacement may be calculated. <br> - Learn in finding approximately unknown value of a function in terms of nearby known values. <br> - Understand conditions under which a given function can be approximated by a simpler series of functions thereby simplifying the study of the function. <br> - Will be familiarised with the conditions under which a given periodic function may be represented in terms of sine/cosine functions. <br> - Learn how maximum/minimum value of a given realvalued function can be found: <br> - Learn to test converging/diverging/oscillatory behaviour of successive values of a real variable. <br> - Will be introduced to the concept of adding countable number of real numbers and thereby testing whether such an expression corresponds to a real number. <br> - Find whether the dependent variable is increasing/decreasing with increase in independent variable value and the rate of Increment/decrement. |


|  | - Become familiar with conditions under which approximate value of a dependent variable may be found when value of the variable and rate of change of that variable at a nearby point are known. <br> - Establish bounds between which an unknown quantity lies. <br> - Learn the method for searching minimum/maximum value of a given dependent variable. <br> - Study properties of geometrical figures through handling of directed line segments. <br> - Study matrices as a means of representing linear maps like geometrical transformations and coordinate changes and how does evaluating determinant associated with a square matrix helps in establishing important properties like invertibility of the matrix. <br> - Will get acquainted with the methods of checking whether a given system of hyperplanes have a common point and, in case it has, to find the common points. <br> - Will get familiarized with the process of writing a system of linear equations in terms of matrices. |
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| Reading/Reference Lists *4 | - Introduction to Real Analysis-Bartle, Sherbert <br> - Real Analysis-S.K.Mapa <br> - Higher Algebra (Linear and Abstract)-S.K.Mapa <br> - Vector Algebra-Maity,Ghosh <br> Online Lectures: <br> - https://youtu.be/nH05UiErAX4 <br> - https://youtu.be/tffrrtzUhmw |
| Evaluation | Theory Practical (if applicable) <br> CIA: $20+5+5=30$ CA: <br> Semester Exam: 70 Semester Exam: |
| Paper Structure for Theory Semester Exam | $\dot{7}$ questions each carrying 10 marks out of 12/13 questions |

