| Semester | 1 |
| :---: | :---: |
| Course *1 | Major-1 |
| Paper Code | C1MT230111T |
| Paper Title | Differential Equations-1 |
| No. of Credits *2 | 4 |
| Theory / Practical / Composite | Theory |
| Minimum No. of preparatory hours per week a student has to devote | 4 |
| Number of Modules | Nil |
| Syllabus | First Order ODE [13]: Genesis of Ordinary differential equations from geometry and other fields [2]. Exact differential equations of first order [2]. Non exact differential equations of first order and integrating factors, linear equation and Bernoulli equations, special integrating factors and transformations.[5] First order ode of higher degree: equations solvable for $\mathrm{x}, \mathrm{y}$ and p . Clairaut's equations and differential equations transformable into Clairaut's form. Singular solutions. [4] <br> Higher order ODE [22]: General solution of linear homogeneous differential equation of second and higher order, principle of superposition. Wronskian to check independency of functions.[4] Linear inhomogeneous equations of higher order with constant coefficients [5] Cauchy-Euler's equation [2] Method of undetermined coefficients [2] Second order differential equations with variable coefficients-finding complementary function in terms of a known integral. Method of variation of parameters to solve inhomogeneous equations [6] Exact higher order ode [3] <br> System of ODE[17]:Reduction of higher order linear differential equations into a system of first order linear differential equations [2] Differential operators, solving a system of homogeneous and non-homogeneous linear ODE's of two variables by operator method [5] Expressing a system of homogeneous linear ODE into $\frac{d \vec{X}}{d t}=A \vec{X}$ form where $\vec{X}$ has there or more component and solving them using eigenvalue[5].Introduction to generalised eigenvector. |
| Learning Outcomes *3 | On successful completion of the course a student will be able to do the following: |


|  | - Investigate real-world framework to realize when ordinary differential equations (ODEs) or systems of ODEs are appropriate, formulate problems mathematically and innovatively model these real-life phenomena to solve the problems and infer if the results are rational, and finally very aptly interpreting the results. <br> - Solve first order ODE's utilizing the standard techniques for separable and exact differential equations. <br> - Identify integrating factors for first order nonexact ODE's and solve them; Linear Equations of first order and Bernoulli's Equations as special cases. <br> - Obtain general solutions of first order higher degree ODE's; Clairaut's Equations in particular; Identification of singular solutions and interpreting them geometrically. <br> - Explore some of the basic theory of linear ODEs, gain ability to recognize certain basic types of higher-order linear ODEs for which exact solutions may be obtained, and to apply the corresponding methods of solution. <br> - Obtain the general solution of nonhomogeneous $2^{\text {nd }}$ and higher order linear differential equations as a linear combination of Complementary Function and Particular Integral. <br> - Obtain the general solution of nonhomogeneous linear ODE with constant coefficients by the method of undetermined coefficients. <br> - Find general solution of $2^{\text {nd }}$ and higher order linear ODE with variable co-efficients by the method of variation of parameters and to solve exact higher order ODE's. <br> - Understand the connection between system of linear equations and system of first order differential equations. <br> - Solve system of ODE's using operator and eigen value method. |
| :---: | :---: |
| Reading/Reference Lists *4 | - S.L. Ross: Differential Equations, 3rd Ed., John Wiley and Sons, India, 2004. |


|  | - G.F.Simmons: Differential Equations with Historical Notes. <br> - TynMyint-U and Lokenath Debnath: Linear Partial Differential Equations for Scientists and Engineers, 4th edition, Springer, Indian reprint, 2006. <br> - Martha L Abell, James P Braselton: Differential Equations with MATHEMATICA, 3rd Ed., Elsevier Academic Press, 2004. <br> - R. Kent Nagle, Edward B. Saff, Arthur David Snider: --Fundamentals of Differential Equations (8 th Ed.),Pearson. <br> - R. Kent Nagle, Edward B. Saff, Arthur David Snider:Fundamentals of Differential Equations (8 th Ed.),Pearson. <br> - D.A.Murray: Differential Equations [Orient Longmann]. <br> - Ghosh \& Chakraborty: Ordinary Differential Equations. Online Lectures: <br> - https://youtu.be/_LX1p0VFkp4 <br> - https://ocw.mit.edu/courses/18-03-differential-equations-spring-2010/ |
| :---: | :---: |
| Evaluation | Theory Practical (if applicable) <br> CIA: $20+5+5=30$ CA: <br> Semester Exam: 70 Semester Exam: |
| Paper Structure for Theory Semester Exam | 7 questions each carrying 10 marks out of 12/13 questions |

