

| <b>Semester: 4</b>  |   |                                   |                      |                        |
|---|---|-----------------------------------|----------------------|------------------------|
| <b>Programme: Data Science</b>  |   |                                   |                      |                        |
| <b>Course: Discrete Structures</b>  |   |                                   |                      |                        |
| <b>Paper code:</b>  |   |                                   | <b>Credits: 4</b>    |                        |
| <b>Hours/week: 4</b>  |   |                                   |                      |                        |
| <b>Category: Core/MDC/SEC/VAC: Core</b>   |   |                                   |                      |                        |
| <b>Theory / Practical / Composite: Theory</b>   |   |                                   |                      |                        |
| <b>No of Module: 1</b>  |   |                                   |                      |                        |
| <b>Course Outcome:</b>  |   |                                   |                      |                        |
| 1. <b>Remember</b> fundamental definitions, terminology, and principles related to counting theory, propositional logic, and graph structures.                              |   |                                   |                      |                        |
| 2. <b>Understand</b> the conceptual framework of recurrence relations, generating functions, and the properties of logical connectives and well-formed formulas.            |   |                                   |                      |                        |
| 3. <b>Apply</b> combinatorial analysis, mathematical induction, and specific graph algorithms, such as Dijkstra's and Kruskal's, to solve discrete mathematical problems.   |   |                                   |                      |                        |
| 4. <b>Analyze</b> the behavior of recurrence relations using the Master Theorem and the structural properties of various graphs, including connectivity and planarity.      |   |                                   |                      |                        |
| 5. <b>Evaluate</b> the validity of mathematical arguments using tautologies and normal forms, and judge the efficiency of different graph algorithm implementations.        |   |                                   |                      |                        |
| 6. <b>Create</b> mathematical models and algorithmic solutions by synthesizing concepts from graph theory and recurrence relations to address complex data science problems |   |                                   |                      |                        |
| <b>SYLLABUS</b>   |   |                                   |                      |                        |
| <b>UNIT/Module</b>  | <b>CONTENT</b>  | <b>HOURS or NUMBER OF CLASSES</b> | <b>CO Mapping</b>    | <b>COGNITIVE LEVEL</b> |
| <b>1.</b>   | <b>Counting Theory:</b> Pigeonhole Principle; Mathematical Induction; Principle of Inclusion and Exclusion.   | <b>8</b>                          | <b>CO1, CO3</b>      | <b>K1, K3</b>          |
| <b>2.</b>   | <b>Recurrence Relations:</b> Formulation, Substitution Method, Linear Recurrence Relations with constant coefficients and their solution, Generating functions, Recurrence Trees, Master Theorem.   | <b>9</b>                          | <b>CO2, CO4, CO6</b> | <b>K2, K4, K6</b>      |
| <b>3.</b>   | <b>Propositional Logic:</b> Logical Connectives, Well-formed Formulas, Tautologies, Equivalences, Normal Forms.   | <b>7</b>                          | <b>CO1, CO5</b>      | <b>K1, K5</b>          |
| <b>4.</b>   | <b>Graph Theory:</b> Definition of Graph, Graph Terminology, Finite and Infinite graphs. Directed and undirected graphs, Degree, Isolated vertex, Pendant vertex. Null graphs. Walks: Paths and circuits. Connected and disconnected graphs, Euler's graphs, Hamiltonian paths and circuits. Planar | <b>13</b>                         | <b>CO1, CO4, CO6</b> | <b>K1, K4, K6</b>      |

|  |  |                                |               |            |
|--|--|--------------------------------|---------------|------------|
|  | Graph, Isomorphic graph, Graph Coloring Problem  |                                |               |            |
| 5.   | <b>Graph Algorithms:</b> Graph representation, Floyd's shortest Path algorithm, Trees, Minimal Spanning Tree using Kruskal Algorithm and Prim's Algorithm, Dijkstra's Algorithm, Breadth First Search (BFS), Depth First Search (DFS), Connected components. | 15                             | CO3, CO5, CO6 | K3, K5, K6 |
| <b>Text Books</b>  |  |                                |               |            |
| 1. C.L. Liu, D.P., Elements of Discrete mathematics, 2nd Edition, Tata McGraw Hill, 1985                       |  |                                |               |            |
| 2. Kenneth Rosen, Discrete Mathematics and Its Applications, Sixth Edition, McGraw Hill 2006                   |  |                                |               |            |
| 3. M. O. Albertson and J. P. Hutchinson, Discrete Mathematics with Algorithms, John wiley Publication, 1988    |  |                                |               |            |
| 4. J. L. Hein, Discrete Structures, Logic, and Computability, 3rd Edition, Jones and Bartlett Publishers, 2009 |  |                                |               |            |
| 5. D.J. Hunter, Essentials of Discrete Mathematics, Jones and Bartlett Publishers                              |  |                                |               |            |
| <b>Evaluation</b>  | Theory CIA: 30<br>Semester Exam: 70<br>Total: 100  |                                |               |            |
| <b>Paper Structure for Theory Semester Exam Module:</b>  | Short questions (5 marks each)   | Long questions (15 marks each) |               |            |
|  | 5 out of 7   | 3 out of 5                     |               |            |

### Course outcomes (COs) and Cognitive Level Mapping

| COs | CO Description   | Cognitive levels |
|-----|--|------------------|
| CO1 | <b>Remember</b> fundamental definitions, terminology, and principles related to counting theory, propositional logic, and graph structures.                              | K1               |
| CO2 | <b>Understand</b> the conceptual framework of recurrence relations, generating functions, and the properties of logical connectives and well-formed formulas.            | K2               |
| CO3 | <b>Apply</b> combinatorial analysis, mathematical induction, and specific graph algorithms, such as Dijkstra's and Kruskal's, to solve discrete mathematical problems.   | K3               |
| CO4 | <b>Analyze</b> the behavior of recurrence relations using the Master Theorem and the structural properties of various graphs, including connectivity and planarity.      | K4               |
| CO5 | <b>Evaluate</b> the validity of mathematical arguments using tautologies and normal forms, and judge the efficiency of different graph algorithm implementations.        | K5               |
| CO6 | <b>Create</b> mathematical models and algorithmic solutions by synthesizing concepts from graph theory and recurrence relations to address complex data science problems | K6               |